Edge Localized Modes

- Fast ($\sim 100 \mu$ s) eruption from the edge of tokamak plasmas
- ▶ If uncontrolled in ITER, these would release $\sim 20~{
 m MJ}$
- World-wide effort to understand and control these events



The BOUT++ Simulation Code

- ▶ Based on BOUT written by X. Xu, et. al. from LLNL [1]
- ▶ New 3D simulation code developed at York with LLNL and ANL
- Simulates plasma fluid equations in curvilinear coordinate systems
- ► Runs on workstations, clusters, large-scale machines, e.g., Cray XE6

ELM Equations

$$\rho_{0} \frac{d\omega}{dt} = B_{0}^{2} b \cdot \nabla \left(\frac{J_{||}}{B_{0}}\right) + 2b_{0} \times \kappa_{0} \cdot \nabla p$$

$$\frac{\partial A_{||}}{\partial t} = -\nabla_{||} \phi$$

$$\frac{dp}{dt} = -\frac{1}{B_{0}} b_{0} \times \nabla \phi \cdot \nabla p_{0}$$

$$\omega = \frac{1}{B_{0}} \nabla_{\perp}^{2} \phi$$

$$J_{||} = J_{||0} - \frac{1}{\mu_{0}} \nabla_{\perp}^{2} A_{||}$$

$$\frac{d}{dt} = \frac{\partial}{\partial t} + \frac{1}{B_{0}} b_{0} \times \nabla \phi \cdot \nabla$$
[3]

References

- [1] BD Dudson et al. "BOUT++: A framework for parallel plasma fluid simulations". In: Computer Physics Communications 180.9 (2009), pp. 1467–1480.
- [2] P Narayanan et al. "Performance Characterization for Fusion Co-design Applications". In: *Proceedings of CUG* (2011).
- [3] XQ Xu et al. "Nonlinear Simulations of Peeling-Ballooning Modes with Anomalous Electron Viscosity and their Role in Edge Localized Mode Crashes". In: *Physical review letters* (2010).



http://www-users.york.ac.uk/~bd512/simulation.shtml#bout

BOUT++: Performance Characterization and Recent Advances in Design

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- ► Time integration and Newton-Krylov nonlinear solves using SUNDIALS (LLNL) or PETSc (ANL)
- Coordinate system and differential operators
- Parallel communications using MPI



SUNDIALS: https://computation.llnl.gov/casc/sundials PETSc: http://www.mcs.anl.gov/petsc

Jacobian-free Newton-Krylov Method

At each timestep, we solve the nonlinear system F(x)=0,

where $F: \mathbb{R}^n \to \mathbb{R}^n$ by a Newton-Krylov method

 $x_{k+1} = x_k - [F'(x_k)]^{-1}F(x_k), \;\; k = 0, 1, \dots,$

where x_0 is an initial approximation to the solution and $F'(x_k)$, the Jacobian, is nonsingular at each iteration. In practice, the Newton iteration is implemented by the following two steps:

> 1. (Approximately) solve $F'(x_k)\Delta x_k = -F(x_k)$. Update $x_{k+1} = x_k + \alpha \Delta x_k$.

where $0 < lpha \leq 1$ is a scalar. Jacobian-vector products in Krylov methods are computed matrix-free via

$$F'(u)approx rac{F(u+h\cdot a)+h}{h}$$

FACETS

- Framework Application for Core-Edge Transport Simulations
- PI: John Cary, http://www.facetsproject.org
- ► FACETS goal: Modeling of a fusion device from the core to the wall
- ► Work in progress: Incorporating BOUT++ as a FACETS component

(a) Mesh

(b) X-Point







-F(u)

Ongoing and Future Work

Research on robust and scalable preconditioners

- Algebraic approaches that use sparse approximate Jacobian information
- Leverage physics knowledge, including field splits for fast Alfven waves, fast magnetosonic waves, and thermal conductivity along the field lines
- Experiments with communication-reducing Krylov methods
- Exploration of IMEX techniques for flexible timestepping
- Incorporation into FACETS and exploration of multiphysics coupling issues
- Research on additional modeling capabilities





cost of MPI_AllReduce() calls inside Newton-Krylov solver are a significant scalability barrier for ELM_pb: nx=516, ny=64, nz=16, global vector dimension: 1,585,152. Data from 10 timesteps, Newton with restarted GMRES, no preconditioning